Modeling and designing intelligent adaptive sliding mode controller for an Eight-Rotor MAV

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Abstract

This paper focuses on the modeling and intelligent control of the new Eight-Rotor MAV, which is used to solve the problem of the low coefficient proportion between lift and gravity for the Quadrotor MAV. The Eight-Rotor MAV is a nonlinear plant, so that it is difficult to obtain stable control, due to uncertainties. The purpose of this paper is to propose a robust, stable attitude control strategy for the Eight-Rotor MAV, to accommodate system uncertainties, variations, and external disturbances. First, an interval type-II fuzzy neural network is employed to approximate the nonlinearity function and uncertainty functions in the dynamic model of the Eight-Rotor MAV. Then, the parameters of the interval type-II fuzzy neural network and gain of sliding mode control can be tuned on-line by adaptive laws based on the Lyapunov synthesis approach, and the Lyapunov stability theorem has been used to testify the asymptotic stability of the closed-loop system. The validity of the proposed control method has been verified in the Eight-Rotor MAV through real-time experiments. The experimental results show that the performance of the interval type-II fuzzy neural network based adaptive sliding mode controller could guarantee the Eight-Rotor MAV control system good performances under uncertainties, variations, and external disturbances. This controller is significantly improved, compared with the conventional adaptive sliding mode controller, and the type-I fuzzy neural network based sliding mode controller.

Key words: Interval type-II fuzzy neural network, sliding mode controller, Eight-Rotor MAV

1. Introduction

Recently, researches on Micro Aerial Vehicles (MAVs) have been vigorously performed for calamity observation, spraying agricultural chemicals, and military purposes, such as reconnaissance, monitoring, and communication. Moreover, the technology of the MAVs is getting faster, according to the rapid progress of electronic and computer technology. MAV are classified into two categories, fixed and rotary wing types. The rotary wing type MAVs are more advantageous than the fixed wing type ones, as regards VTOL (Vertical Take-off and Landing), omni-directional flying, and hovering performance. Rotary wing type MAVs are classified into quad-rotor type (QRT), co-axial helicopter, and helicopter etc. QRT MAVs

have the simplest mechanical structure among them, and the quadrotor we consider to be an underactuated system, with six outputs and four inputs, where the states are highly coupled. To deal with this problem, many modeling approaches have been presented [1, 2], and various control methods proposed [3-7]. Bouabdallah et al. presented PID vs. LQ control techniques applied to an indoor MicroQuadrotor [3]. Tayebi et al. studied attitude stabilization of a VIOL quadrotor aircraft [4]. Another PD control method was proposed by Erginer et al. [5]. Feedback Linearization vs. Adaptive Sliding Mode Control for a Quadrotor Helicopter was implemented by Lee et al. [6]. A new robust adaptive-fuzzy control method applied to quadrotor helicopter stabilization was proposed by Coza et al. [7].

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Of course, the whole purpose of the MAV is to carry a payload. For the moment, the primary mission assigned to MAVs is aerial observation and surveillance. MAVs are obviously an advantageous solution for missions where a live crew offers no real benefits, or where the risks are too high. In general, for MAVs to carry out the missions under consideration, all aspects of the system will have to be improved: the vehicle itself, payloads, and in particular, sensors, transmission systems, and onboard intelligence.

In this paper, we introduce a configuration of a multi rotor helicopter composed of eight rotors, which is used to solve the problem of the low coefficient proportion between lift and gravity of the Quadrotor MAV. The main characteristics of the configurations are increased payload capacity, quietness efficiency, stability in the wind, and damage tolerance.

A dynamic model is presented. To validate the model, we introduce an intelligent control strategy, and apply it in real-time experiences. The control strategy is based on a Neuro-Fuzzy adaptive controller. Neuro-Fuzzy has been used in a lot of successful applications [8-13]. For example, Spooner et al. [8] and Ordonez et al. [9] proposed a combination of fuzzy systems and neural networks to make adaptive control systems. Melin et al. used a neuro-fuzzy-fractal approach to adaptive control of a model-based non-linear dynamic plant [10]. Lou et al. used a neuro-fuzzy method for modeling and adaptive control of the mechanism [11]. Melin et al. used a neuro-fuzzy-genetic approach to the control of complex electrochemical systems [12]. Er et al. designed a dynamic fuzzy neural networks controller for a Selective Compliance Assembly Robot Arm and (SCARA) with real-time implementation [13]. But these are based on type-I fuzzy sets. With the higher control accuracy requirements, the type-II fuzzy neural network [14-17] that has been developed recently, has better performances than the type-I fuzzy neural network. For example, system identification by using a type-II fuzzy neural network was developed by Lee et al. [14], and Wang studied dynamic optimal training for interval type-II fuzzy neural networks [15]. A double axis motion control system and dynamic time-varying system identification with type-II fuzzy neural networks was designed by Chen et al. [16-17]. This paper is to apply type-II fuzzy neural networks to control the attitude of the Eight-Rotor MAV.

More recently, there are many papers discussing how to improve the stability of fuzzy-neural controllers. It is well known that sliding mode control provides a robust means for controlling a nonlinear dynamic system with uncertainties. Lin [18] proposed an interval type-II fuzzy-neural network direct adaptive sliding mode control for SISO nonlinear systems. In this paper, we develop a gain adaptive sliding mode controller based on an interval type-II fuzzy neural network [18-20] identification and Lyapunov synthesis approach for the

Eight-Rotor MAV, which is a MIMO nonlinear system. By introducing an interval type-II fuzzy neural network to approximate the unknown nonlinear functions of the dynamic systems, through tuning by the desired adaptive law, we introduce the Lyapunov synthesis technique in this paper. Furthermore, by incorporating the Lyapunov design approach and sliding mode control method into the adaptive fuzzy-neural control scheme to derive the control law, the advocated design methodology not only assures closed-loop stability, but also a desired tracking performance can be achieved for the overall system, based on a much relaxed assumption.

This paper is organized as follows: the attitude dynamic model of the Eight-Rotor MAV is given in Section 2. A brief illustration of an interval type-II fuzzy neural network is presented in Section 3. A gain adaptive sliding mode controller based on interval type-II fuzzy neural network identification is constructed in Section 4, which is also devoted to the stability analysis of the control scheme. A platform description and some experiences are given in Section 5, and Section 6 contains concluding remarks.

2. Dynamic modelling of the Eight-Rotor MAV

The EightRotor is very well modeled, with eight rotors in a cross configuration. This cross structure is quite thin and light; however, it shows robustness, by mechanically linking the motors. Each propeller is connected to the motor through reduction gears. All the propellers axes of rotation are fixed and parallel. These considerations point out that the structure is quite rigid, and the only things that can vary are the propeller speeds. Neither the motors nor the reduction gears are fundamental, because the movements are directly related just to the propellers velocities, as can be seen in Fig. 1.

The first step before control development is an adequate dynamic system modeling. Let us consider two frames that have to be defined: the earth inertial frame (E-frame) [10]; and the body-fixed frame (B-frame). Eq. (1) describes the

Fig. 1. Flight theory of Eight-Rotor MAV

kinematics of a generic 6 degree of freedom rigid-body:

$$\dot{\eta} = \begin{bmatrix} R & 0_{3 \times 3} \\ 0_{3 \times 3} & T \end{bmatrix} v \quad (1)$$

where, the η means orientation and position of the Eight-Rotor MAV with respect to the inertial reference frame; while the v means the linear and angular velocities of orientation and position of Eight-Rotor MAV with respect to the body-fixed frame, x, y, z represent the linear positions, and ϕ, θ, ψ represent the roll, pitch and yaw angles in the inertial reference frame, respectively. η and v are shown in Eqs. (2) and (3).

$$\eta = [x \ y \ z \ \phi \ \theta \ \psi]^T \quad (2)$$

$$v = [u \ v \ w \ p \ q \ r]^T \quad (3)$$

The notation $0_{3 \times 3}$ means a sub-matrix with dimension 3 times 3 filled with all zeros, while the rotation R and the transfer T matrices are defined according to Eqs. (4) and (5).

$$R = \begin{bmatrix} c\psi c\theta & -s\psi c\theta + c\psi s\theta s\phi & s\psi s\theta + c\psi s\theta c\phi \\ s\psi c\theta & c\psi c\theta + s\psi s\theta s\phi & -c\psi s\theta + s\psi s\theta c\phi \\ -s\theta & c\theta s\phi & c\theta c\phi \end{bmatrix} \quad (4)$$

$$T = \begin{bmatrix} 1 & s\phi \tan \theta & c\phi \tan \theta \\ 0 & c\phi & -s\phi \\ 0 & s\phi / c\theta & c\phi / c\theta \end{bmatrix} \quad (5)$$

The dynamics of a generic 6 degree of freedom rigid-body take into account the mass of the body m and its inertia matrix I , which is calculated in this work. The dynamics are described by Eq.(6)

$$\begin{bmatrix} mI_{3 \times 3} & 0_{3 \times 3} \\ 0_{3 \times 3} & I \end{bmatrix} \begin{bmatrix} \dot{v} \\ \dot{\omega} \end{bmatrix} + \begin{bmatrix} \omega \times mV \\ \omega \times I\omega \end{bmatrix} = \begin{bmatrix} F^B \\ \tau^B \end{bmatrix} \quad (6)$$

where, the notation $I_{3 \times 3}$ means a 3 times 3 identity matrix. V is the Eight-Rotor linear speed vector, while ω is the Eight-Rotor angular speed. In addition, F^B is the Eight-Rotor forces vector, and τ^B is the quadrotor torque vector with respect to the B-frame. A generalized force vector A can be defined according to equation Eq. (7).

$$\Gamma = \begin{bmatrix} F^B & \tau^B \end{bmatrix} = \begin{bmatrix} F_x & F_y & F_z & \tau_x & \tau_y & \tau_z \end{bmatrix}^T \quad (7)$$

Hence the last vector contains specific information about its dynamics. Γ can be divided into three components, according to the nature of the Eight-Rotor contributions.

The first contribution is the gravitational vector $G_B(\xi)$, given from the acceleration due to gravity g . It is easy to understand that it affects just the linear, and not the angular equations, since it's a force, and not a torque. Eq. (8) shows the transformations to get $G_B(\xi)$.

$$G_B = \begin{bmatrix} F^B \\ 0_{3 \times 1} \end{bmatrix} = \begin{bmatrix} R^{-1} F^E \\ 0_{3 \times 1} \end{bmatrix} = \begin{bmatrix} mgs\theta \\ -mgc\theta s\phi \\ -mgc\theta c\phi \\ 0 \\ 0 \\ 0 \end{bmatrix} \quad (8)$$

where F^B the gravitational force is a vector with respect to the B-frame, and F^E is that one with respect to the E-frame. Furthermore, since R is an orthogonal normalized matrix, its inverted R^{-1} is equal to the transposed one R^T .

The second contribution takes into account the gyroscopic effects produced by the propeller rotation, since four of them are rotating clockwise, and the other four counter clockwise. The overall rotor speeds are, in general, not equal to zero. In imbalance, when the algebraic sum of the addition, roll or pitch rates are also different from zero, the Eight-Rotor experiences a gyroscopic torque, according to Eq. (9). $O_B(v)$ is the gyroscopic propeller matrix, and J_T is the total rotational moment of inertia around the propeller axis calculated in the next section. It is easy to see that the gyroscopic effects produced by the propeller rotation are just related to the angular, and not the linear, equations.

$$O_B(v)\Omega = \left[-\sum_{i=1}^8 J_T \begin{bmatrix} 0_{3 \times 1} \\ \omega \times \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix} \end{bmatrix} (-1)^i \Omega_i \right] \quad (9)$$

The third contribution takes into account the forces and torques directly produced by the main movement inputs. From aerodynamic consideration, it follows that both forces and torques are proportional to the squared propellers' speed. Therefore the movement matrix E_B is multiplied by Ω^2 to get the movement vector U_B , where $\Omega_i (i=1, 2, \dots, 6)$ is in respect to the speed of Rotor i th. This can be expanded, to move the Eight-Rotor platform in any combination of yaw, roll, and pitch. Because the Eight-Rotor can be controlled by simply varying the speed of 8 motors, it is a very mechanically simple platform. Eq. (10) shows the action of the movement vector on the Eight-Rotor helicopter dynamics.

$$U_B = \begin{bmatrix} 0 \\ 0 \\ b \left((\Omega_1 + \Omega_2)^2 + (\Omega_3 + \Omega_4)^2 \right) \\ b \left((\Omega_5 + \Omega_6)^2 + (\Omega_7 + \Omega_8)^2 \right) \\ dl \left((\Omega_1 + \Omega_2)^2 - (\Omega_5 + \Omega_6)^2 \right) \\ dl \left((\Omega_7 + \Omega_8)^2 - (\Omega_3 + \Omega_4)^2 \right) \\ dl \left((\Omega_7 + \Omega_8)^2 + (\Omega_3 + \Omega_4)^2 \right) \\ dl \left(-((\Omega_1 + \Omega_2)^2 - (\Omega_5 + \Omega_6)^2) \right) \end{bmatrix} \quad (10)$$

where, l is the distance between the center of the Eight-Rotor

and the center of a propeller, b means the square of the motor speed-lift scaling factor, d means the force-moment scaling factor, and U_1, U_2, U_3 and U_4 are the movement vector components. Their relation with the propeller speeds comes from aerodynamic calculus. Therefore, all the movements have a similar expression, and are easier to control. It is possible to describe the Eight-Rotor dynamics considering these last three contributions, according to Eq. (11).

$$\Gamma = G_B(\xi) + O_B(v)\Omega + E_B\Omega^2 \quad (11)$$

Eq. (12) shows the previous expression not in a matrix form, but in a system of equations:

$$\begin{cases} m\ddot{x} = (s\psi s\phi + c\psi c\theta)U_1 \\ m\ddot{y} = (-c\psi s\phi + s\theta s\psi c\theta)U_1 \\ m(\ddot{z} + g) = c\theta c\phi U_1 \\ I_x\dot{\omega}_x + (I_z - I_y)\omega_y\omega_x = U_2 \\ I_y\dot{\omega}_y + (I_x - I_z)\omega_z\omega_x = U_3 \\ I_z\dot{\omega}_z = U_4 \end{cases} \quad (12)$$

where, the propellers' speed inputs are given through Eq.(13)

$$\begin{cases} U_1 = b((\Omega_1 + \Omega_2)^2 + (\Omega_3 + \Omega_4)^2 \\ \quad + (\Omega_5 + \Omega_6)^2 + (\Omega_7 + \Omega_8)^2) \\ U_2 = dl((\Omega_1 + \Omega_2)^2 - (\Omega_5 + \Omega_6)^2) \\ U_3 = dl((\Omega_7 + \Omega_8)^2 - (\Omega_3 + \Omega_4)^2) \\ U_4 = dl(((\Omega_7 + \Omega_8)^2 + (\Omega_3 + \Omega_4)^2) \\ \quad - ((\Omega_1 + \Omega_2)^2 + (\Omega_5 + \Omega_6)^2)) \end{cases} \quad (13)$$

The dynamics of the Eight-Rotor are well described in the previous section. However the most important concepts can be summarized in Eqs. (12) and (13). The first one shows how the Eight-Rotor accelerates, according to the basic movement commands given. The second equation explains how the basic movements are related to the propellers' squared speed. The goal of the Eight-Rotor stabilization is to find those values of the motors' voltage that maintain the helicopter in a certain position required in the task. This process is also known as inverse kinematics and inverse dynamics. Unlike the direct ones, the inverse operations are not always possible, and are not always unique. For these reasons, their consideration is much more complicated.

Making the outputs tracks the attitude of the Eight-Rotor MAV, by designing the control torque U . Arranging the above dynamic equations for designing the control scheme conveniently, the attitude control model of the Micro Aircraft Vehicle obtained can be expressed as:

$$\begin{cases} \dot{x}_1 = bT \\ \dot{T} = F(T) + U + d \\ y = x_1 \end{cases} \quad (14)$$

where, $\varphi = [\theta \ \psi \ \phi]^T$, $w = [q \ r \ p]^T$,

$$F(T) = \begin{bmatrix} \frac{(I_x - I_z)pr}{I_y} & \frac{(I_x - I_y)pq}{I_z} & \frac{(I_z - I_y)qr}{I_x} \end{bmatrix}^T,$$

$$U = [U_2 \ U_3 \ U_1]^T, b(x_1) = \begin{bmatrix} \cos\phi & -\sin\phi & 0 \\ \sin\phi/\cos\theta & \cos\phi/\cos\theta & 0 \\ \sin\phi\tan\theta & \cos\phi\tan\theta & 1 \end{bmatrix}.$$

Next, we propose $x = bt$ and $f = \dot{b}F(T) + bT$, the control model turned to, as following eventually:

$$\begin{cases} \ddot{x} = f + \tilde{f} + (b + \tilde{b})U + d \\ y = x \end{cases} \quad (15)$$

where, $x_1, x_2, x \in R^3$ denotes the controlled state vector, $F, f \in R^3$ means the system function vector, $b \in R^{3 \times 3}$ means the control coefficient matrix, $U \in R^3$ means the control input matrix vector, $d \in R^3$ means the disturbance vector, $y \in R^3$ means the control output vector, $\tilde{f}, \tilde{b} \in R^{3 \times 3}$ means the uncertainty function vector caused by attitude perturbations, and each component expression of $f = [f_1 \ f_2 \ f_3]^T$ is referred to as:

$$\begin{cases} f_1 = (p + q \tan\theta \sin\phi + r \tan\theta \cos\phi)(-r \cos\phi - q \sin\phi) - \frac{I_x - I_y}{I_z} pq \sin\phi \\ \quad + \frac{I_z - I_x}{I_y} rp \cos\phi \\ f_2 = \frac{1}{\cos\theta} ((p + q \tan\theta \sin\phi + r \tan\theta \cos\phi)(q \cos\phi - r \sin\phi) + \frac{I_x - I_y}{I_z} pq \sin\phi \\ \quad + \tan\theta(q \sin\phi + r \cos\phi)(q \sin\phi - r \cos\phi) + \frac{I_z - I_x}{I_y} rp \cos\phi) \\ f_3 = + \frac{I_y - I_z}{I_x} rq + \frac{I_x - I_y}{I_z} pq \cos\phi \tan\theta + \frac{I_z - I_x}{I_y} rp \sin\phi \tan\theta \\ \quad + \tan\theta(p + q \tan\theta \sin\phi + r \tan\theta \cos\phi)(q \cos\phi - r \sin\phi) \\ \quad + \frac{1}{\cos^2\theta} (q \sin\phi + r \cos\phi)(q \sin\phi - r \cos\phi) \end{cases} \quad (16)$$

Aerodynamic characteristics parameters will get perturbations, resulting from flying conditions or changes in flying attitude. At the same time, external gusts of wind and flow cannot be ignored. Thus, the control system of the Micro Aircraft Vehicle is a MIMO nonlinear system with uncertainty and perturbations.

3. Introduction of the Interval Type-II Fuzzy Neural Network

The structure of ITIIFNN [16-17] is depicted in Fig. 2; each rule in ITIIFNN is of the first Takagi-Sugeno-Kang (TSK) type. The detailed mathematical functions of each layer are introduced as follows:

Layer 1 (Input layer): This layer defines the input variables that first enter the ITIIFNN.

Layer 2 (Membership layer): In this layer, each node performs an interval type-II fuzzy MF. The FOU of this MF can be represented as an interval, bound by lower MF $\underline{\mu}_i^j(x_i)$ and upper MF $\overline{\mu}_i^j(x_i)$:

Fig. 2. The structure of IT-IIFNN

$$\bar{\mu}_i^j(x_i) = \begin{cases} N(\underline{\zeta}_i^j, \sigma_i^j, x_i), & x_i < \underline{\zeta}_{ji}^j \\ 1, & \underline{\zeta}_i^j \leq x_i < \bar{\zeta}_i^j \\ N(\bar{\zeta}_i^j, \sigma_i^j, x_i), & x_i > \bar{\zeta}_i^j \end{cases} \quad (17)$$

$$\underline{\mu}_i^j(x_i) = \begin{cases} N(\underline{\zeta}_i^j, \sigma_i^j, x_i), & x_i \leq \frac{\underline{\zeta}_i^j + \bar{\zeta}_i^j}{2} \\ N(\bar{\zeta}_i^j, \sigma_i^j, x_i), & x_i > \frac{\underline{\zeta}_i^j + \bar{\zeta}_i^j}{2} \end{cases}$$

where, $\zeta_i^j \in [\underline{\zeta}_i^j, \bar{\zeta}_i^j]$ and σ_i^j are, respectively, the mean and the standard deviation of the Gaussian MF of the j th partition for the i th input variable x_i . That is, the output of each node can be represented as an interval $[\underline{\mu}_i^j, \bar{\mu}_i^j]$.

Layer 3 (Rule layer): Each node in this layer corresponds to one fuzzy rule, and performs a fuzzy meet operation, to obtain a firing strength F^i , which is computed as follows:

$$F^i = [\underline{f}^i, \bar{f}^i] = [\prod_{j=1}^n \bar{\mu}_{ji}, \prod_{j=1}^n \mu_{ji}] \quad (18)$$

Layer 4 (Type-reduction layer): This layer is used to implement the type-reduction, and the center-of-sets type reduction method is adopted here. The centroid of the type-II fuzzy set that can be represented by $[\omega_l^j, \omega_r^j]$, which represents link weights, should be set first, before the computation of y_l, y_r . The outputs y_l, y_r can be computed using Kamik-Mendel iterative algorithms, as:

$$y_l = \frac{\sum_{j=1}^L \underline{f}^j w_l^j + \sum_{j=L+1}^N \bar{f}^j w_l^j}{\sum_{j=1}^L \underline{f}^j + \sum_{j=L+1}^N \bar{f}^j} = W_l^T g_l \quad (19)$$

$$y_r = \frac{\sum_{j=1}^R \underline{f}^j w_r^j + \sum_{j=R+1}^N \bar{f}^j w_r^j}{\sum_{j=1}^R \underline{f}^j + \sum_{j=R+1}^N \bar{f}^j} = W_r^T g_r \quad (20)$$

where, $W_r = [\omega_r^1, \dots, \omega_r^N]^T$, $W_l = [\omega_l^1, \dots, \omega_l^N]^T$ and

$$g_l = \left[\frac{f_l^1}{\sum_{i=1}^N f_l^i}, \frac{f_l^2}{\sum_{i=1}^N f_l^i}, \dots, \frac{f_l^N}{\sum_{i=1}^N f_l^i} \right]^T \quad (21)$$

$$g_r = \left[\frac{f_r^1}{\sum_{i=1}^N f_r^i}, \frac{f_r^2}{\sum_{i=1}^N f_r^i}, \dots, \frac{f_r^N}{\sum_{i=1}^N f_r^i} \right]^T$$

Layer 5 (Output layer): Each output node corresponds to one output variable, and acts as a defuzzifier. Hence, the defuzzified output is shown as:

$$y = \frac{y_l + y_r}{2} = \frac{1}{2} (W_l^T g_l + W_r^T g_r) = W^T g(x, \zeta, \sigma) \quad (22)$$

Remark: Initially, there are no fuzzy rules in ITIIFNN. All of the rules are generated online by the structure learning, which not only helps automate rule generation, but also locates good initial rule positions for subsequent parameter learning. Furthermore, the structure and parameter adjustment are performed simultaneously.

4. ASMC- ITIIFNN

To begin with, our objective is to use the ITIIFNN, as shown in Fig. 3, to approximate the uncertainty function f and non-linear function b , for the adaptive sliding model controller

Table 1. Response data of three attitude angles

	Regulation time (ms)	Overshoot (%)	Steady-state error (°)
Yaw1	180/245	14/24.5	0.15/0.25
Yaw2	175/220	9.5/17	0.08/0.30
Yaw3	145/150	4.5/14	0.02/0.03
Pitch1	205/240	15.5/18.5	0.075/0.15
Pitch2	150/175	12.5/17.5	0.045/0.25
Pitch3	120/145	1.5/4.0	0.030/0.05
Roll1	190/250	8.8/28	0.04/0.25
Roll2	185/210	4.4/18	0.01/0.40
Roll3	100/120	1/3	0.01/0.02

on-line. Then, we analyze the stability of the proposed adaptive sliding model controller based on ITIIFNN through the Lyapunov stability theorem, in the meantime tuning the parameters of the interval type-II fuzzy neural network and gain of the sliding mode control on-line, by adaptive laws based on the Lyapunov synthesis approach.

4.1 GASMC Design

Proposing y_d is the desired trajectory, and defining

$$E = [e, \dot{e}, \ddot{e}, \dots, e^{(n-1)}]^T = [y_d - y, \dot{y}_d - \dot{y}, \dots, y_d^{(n-1)} - y^{(n-1)}]^T$$

then, the error dynamic equation with uncertainty and external disturbances can be expressed as:

$$\dot{E} = \Lambda E + B\{k^T E + y_d^{(n)} - f_0 - \hat{f}_\Delta - (b_0 + \hat{b}_\Delta)u - d\} \quad (23)$$

where,

$$\Lambda = \begin{bmatrix} 0 & 1 & 0 & 0 & \dots & 0 & 0 \\ 0 & 0 & 1 & 0 & \vdots & 0 & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ -k_n & -k_{n-1} & -k_{n-2} & -k_{n-3} & \dots & -k_2 & -k_1 \end{bmatrix} B = \begin{bmatrix} 0 \\ 0 \\ \vdots \\ 0 \\ 1 \end{bmatrix} \quad (24)$$

In the meantime, the selection of $k = [k_n, k_{n-1}, \dots, k_1]^T$ should make sure that $s^n + k_1 s^{n-1} + \dots + k_n$ is a Hurwitz polynomial.

Taking $x = [\phi, \theta, \psi]^T$ as the input of the ITIIFNN to approximate the uncertainty function f and nonlinear function b on-line, we replace f and b by ITIIFNN as:

$$\begin{aligned} \hat{f}_\Delta(x | \mathcal{G}_{f\Delta}) &= W_{f\Delta}^T g_{f\Delta}(x, \zeta, \sigma) \\ \hat{b}_\Delta(x | \mathcal{G}_{b\Delta}) &= W_{b\Delta}^T g_{b\Delta}(x, \zeta, \sigma) \end{aligned} \quad (25)$$

Proposing that $f_\Delta^* = \hat{f}_\Delta(x | \mathcal{G}_{f\Delta}^*)$, $b_\Delta^* = \hat{b}_\Delta(x | \mathcal{G}_{b\Delta}^*)$ with respect to the optimal estimations of $\hat{f}_\Delta$, $\hat{b}_\Delta$, the minimum estimation

error is defined as:

$$f_\Delta^* - f_\Delta = E_{f\Delta}, b_\Delta^* - b_\Delta = E_{b\Delta} \quad (26)$$

where, $\mathcal{G}_\#$ respects the adjustable parameters, including the Gaussian membership function mean $\zeta_i^j \in [\underline{\zeta}_i^j, \bar{\zeta}_i^j]$, Gaussian membership function standard deviation σ_i^j , neural network weight $[W_i^j, W_r^j]$, and $\#$ means f_Δ, b_Δ . Then, expand $\hat{f}_\Delta(x | \mathcal{G}_{f\Delta}^*)$, $\hat{b}_\Delta(x | \mathcal{G}_{b\Delta}^*)$ in the Taylor series expression near $\theta_{f\Delta}, \theta_{b\Delta}$:

$$\begin{aligned} \hat{f}_\Delta(x | \mathcal{G}_{f\Delta}) - \hat{f}_\Delta(x | \mathcal{G}_{f\Delta}^*) &= \Phi_{f\Delta}^T \left(\frac{\partial \hat{f}_\Delta(x | \mathcal{G}_{f\Delta})}{\partial \mathcal{G}_{f\Delta}} \right) + O(|\Phi_{f\Delta}|^2) \\ \hat{b}_\Delta(x | \mathcal{G}_{b\Delta}) - \hat{b}_\Delta(x | \mathcal{G}_{b\Delta}^*) &= \Phi_{b\Delta}^T \left(\frac{\partial \hat{b}_\Delta(x | \mathcal{G}_{b\Delta})}{\partial \mathcal{G}_{b\Delta}} \right) + O(|\Phi_{b\Delta}|^2) \end{aligned} \quad (27)$$

where, $\Phi_{f\Delta} = \mathcal{G}_{f\Delta} - \mathcal{G}_{f\Delta}^*$, $\Phi_{b\Delta} = \mathcal{G}_{b\Delta} - \mathcal{G}_{b\Delta}^*$, $\dot{\Phi}_{b\Delta} = \dot{\mathcal{G}}_{b\Delta}$ and $O(|\Phi_{f\Delta}|^2), O(|\Phi_{b\Delta}|^2)$ are representative of the higher-order

item. Each item of $\frac{\partial \hat{f}_\Delta(x | \mathcal{G}_{f\Delta})}{\partial \mathcal{G}_{f\Delta}}$ is expressed as:

$$\begin{aligned} \frac{\partial \hat{f}_\Delta}{\partial w_{lr}} \Big|_k &= \frac{\bar{y}_{f\Delta}^j - \hat{f}_\Delta}{\sum_{j=1}^N f_{lr}^j} \times f_{lr}^j \\ \frac{\partial \hat{f}_\Delta}{\partial \underline{\zeta}_i^j} \Big|_k &= \frac{\frac{1}{2} \frac{\bar{y}_{f\Delta}^j - \hat{f}_\Delta}{\sum_{j=1}^N f_{lr}^j} \left[\frac{w_{lr}^j - y_{lr}}{\sum_{j=1}^N f_{lr}^j} * \left(x(k-1) - \underline{\zeta}_i^j(k-1) \right) \right] \times f_{lr}^j}{(\sigma_i^j(k-1))^2} \\ \frac{\partial \hat{f}_\Delta}{\partial \bar{\zeta}_i^j} \Big|_k &= \frac{\frac{1}{2} \frac{\bar{y}_{f\Delta}^j - \hat{f}_\Delta}{\sum_{j=1}^N f_{lr}^j} \left[\frac{w_{lr}^j - y_{lr}}{\sum_{j=1}^N f_{lr}^j} * \left(x(k-1) - \bar{\zeta}_i^j(k-1) \right) \right] \times f_{lr}^j}{(\sigma_i^j(k-1))^2} \\ \frac{\partial \hat{f}_\Delta}{\partial \sigma_i^j} \Big|_k &= \frac{\frac{1}{2} \frac{\bar{y}_{f\Delta}^j - \hat{f}_\Delta}{\sum_{j=1}^N f_{lr}^j} \left[\frac{w_{lr}^j - y_{lr}}{\sum_{j=1}^N f_{lr}^j} * \left(x(k-1) - \bar{\zeta}_i^j(k-1)^2 \right) \right] \times f_{lr}^j}{(\sigma_i^j(k-1))^3} \end{aligned} \quad (28)$$

Replacing the f_Δ with b_Δ , $\frac{\partial \hat{b}_\Delta(x | \mathcal{G}_{b\Delta})}{\partial \mathcal{G}_{b\Delta}}$ can be achieved. Hence, we obtain:

$$\begin{aligned} \hat{f}_\Delta - f_\Delta &= \hat{f}_\Delta - f_\Delta^* + f_\Delta^* - f_\Delta = \Phi_{f\Delta}^T \left(\frac{\partial \hat{f}_\Delta}{\partial \mathcal{G}_{f\Delta}} \right) + O(|\Phi_{f\Delta}|^2) + E_{f\Delta} \\ \hat{b}_\Delta - b_\Delta &= \hat{b}_\Delta - b_\Delta^* + b_\Delta^* - b_\Delta = \Phi_{b\Delta}^T \left(\frac{\partial \hat{b}_\Delta}{\partial \mathcal{G}_{b\Delta}} \right) + O(|\Phi_{b\Delta}|^2) + E_{b\Delta} \end{aligned} \quad (29)$$

Then,

$$\begin{aligned} -f_\Delta &= -\hat{f}_\Delta + \Phi_{f\Delta}^T \left(\frac{\partial \hat{f}_\Delta}{\partial \mathcal{G}_{f\Delta}} \right) + O(|\Phi_{f\Delta}|^2) + E_{f\Delta} \\ -b_\Delta &= -\hat{b}_\Delta + \Phi_{b\Delta}^T \left(\frac{\partial \hat{b}_\Delta}{\partial \mathcal{G}_{b\Delta}} \right) + O(|\Phi_{b\Delta}|^2) + E_{b\Delta} \end{aligned} \quad (30)$$

Fig. 3. Architecture of ASMC algorithm based on ITIIFNN

By using Eq. (21), Eq. (14) can be rewritten as:

$$\begin{aligned} \dot{E} = & \Lambda E + B\{k^T E + y_d^{(n)} - \hat{f}_0 - \hat{f}_\Delta + O(|\Phi_{f\Delta}|^2) \\ & + E_{f\Delta} - (b_0 + b_\Delta)u + \Phi_{b\Delta}^T \left(\frac{\partial \hat{b}_\Delta}{\partial g_{b\Delta}} \right) + O(|\Phi_{b\Delta}|^2) + E_{b\Delta} \} u - d \end{aligned} \quad (31)$$

Define

$$u^* = k^T E + y_d^{(n)} - \hat{f}_0 - \hat{f}_\Delta - (b_0 + \hat{b}_\Delta)u \quad (32)$$

Then, the error dynamic Eq. (22) could be simplified as:

$$\begin{aligned} \dot{E} = & \Lambda E + B\{u^* + \Phi_{f\Delta}^T \left(\frac{\partial \hat{f}_\Delta}{\partial g_{f\Delta}} \right) + O(|\Phi_{f\Delta}|^2) + E_{f\Delta} \\ & + [\Phi_{b\Delta}^T \left(\frac{\partial \hat{b}_\Delta}{\partial g_{b\Delta}} \right) + O(|\Phi_{b\Delta}|^2) + E_{b\Delta}] u - d \end{aligned} \quad (33)$$

Owing to the given Λ, B , and the parameters in the Eq. (32) are also known, through identification by ITIIFNN, so the nominal system of the error dynamic Eq. (33) is deemed as:

$$\dot{E} = \Lambda E + B u^* \quad (34)$$

where, Λ is a stable matrix. In view of the value principle of K, there exists positive symmetric matrices Q , which guarantees the unique positive symmetric solution P of the Lyapunov equation.

$$\Lambda^T P + P \Lambda = -Q \quad (35)$$

Defining the switching surface as:

$$\sigma = S E \quad (36)$$

where, $S = B^T P$, and we have:

$$\dot{\sigma} = S \Lambda E + S B u_{eq} = 0 \quad (37)$$

Then the equivalent control variable u_{eq} by the nominal system Eq. (34) can be settled as:

$$u_{eq} = (SB)^{-1} S \Lambda E \quad (38)$$

when $u^* = u_{eq}$, we can obtain that:

$$u_c = (b_0 + \hat{b}_\Delta)^{-1} (k^T E + y_d^{(n)} - \hat{f}_0 - \hat{f}_\Delta - (SB)^{-1} S \Lambda E) \quad (39)$$

$$h_{10} = \Phi_{f\Delta}^T \frac{\partial \hat{f}_\Delta}{\partial g_{f\Delta}} + \Phi_{b\Delta}^T \frac{\partial \hat{b}_\Delta}{\partial g_{b\Delta}} u_c \quad (40)$$

$$h_{20} = O(|\Phi_{f\Delta}|^2) + E_{f\Delta} + [O(|\Phi_{b\Delta}|^2) + E_{b\Delta}] u_c - d$$

when $u^* \neq u_{eq}$, set the following expression:

$$u = u_c + \tilde{u}$$

In this time, Eq. (40) turns to be:

$$\begin{aligned} h_{11} = & \Phi_{f\Delta}^T \frac{\partial \hat{f}_\Delta}{\partial g_{f\Delta}} + \Phi_{b\Delta}^T \frac{\partial \hat{b}_\Delta}{\partial g_{b\Delta}} u_c + \Phi_{b\Delta}^T \frac{\partial \hat{b}_\Delta}{\partial g_{b\Delta}} \tilde{u} \\ h_{21} = & O(|\Phi_{f\Delta}|^2) + E_{f\Delta} + [O(|\Phi_{b\Delta}|^2) \\ & + E_{b\Delta}] u_c + [O(|\Phi_{b\Delta}|^2) + E_{b\Delta}] \tilde{u} - d \end{aligned} \quad (41)$$

Taking $\Phi_{b\Delta}^T \frac{\partial \hat{b}_\Delta}{\partial g_{b\Delta}} \tilde{u}$ and $[O(|\Phi_{b\Delta}|^2) + E_{b\Delta}] \tilde{u}$ as the disturbances, and substituting them into the disturbance item d in Eq. (40), the expression is shown as:

$$d_t = d - [O(|\Phi_{b\Delta}|^2) + E_{b\Delta}] \tilde{u} - \Phi_{b\Delta}^T \frac{\partial \hat{b}_\Delta}{\partial g_{b\Delta}} \tilde{u} \quad (42)$$

Then,

$$\begin{aligned} h_{11} = h_{10} = & \Phi_{f\Delta}^T \frac{\partial \hat{f}_\Delta}{\partial g_{f\Delta}} + \Phi_{b\Delta}^T \frac{\partial \hat{b}_\Delta}{\partial g_{b\Delta}} u_c \\ h_{21} = & O(|\Phi_{f\Delta}|^2) + E_{f\Delta} + [O(|\Phi_{b\Delta}|^2) + E_{b\Delta}] u_c - d_t \end{aligned} \quad (43)$$

Now, Eq. (34) can be expressed as:

$$\dot{E} = \Lambda E + B\{u^* + h_1 + h_2\} \quad (44)$$

Next, make the following assumptions:

$$\begin{aligned} d_t & \leq d_0 \\ |E_{f\Delta}| & \leq w_{fd}, |O(|\Phi_{f\Delta}|^2)| + w_{fd} + d_0 \leq \varepsilon_{fd} \\ |E_{b\Delta}| & \leq w_b, |O(|\Phi_{b\Delta}|^2)| + w_{b\Delta} \leq \varepsilon_b \end{aligned} \quad (45)$$

If the above assumptions hold true, the following equation can be obtained as:

$$|h_2| \leq \varepsilon_{fd} + \varepsilon_b u_c = K_{smc}^* \gamma \quad (46)$$

where, $K_{smc}^* = [\varepsilon_{fd} \quad \varepsilon_b]^T$, $\gamma = [1 \quad |u_c|]$.

For enhancing the system robustness with the existences both h_1 and h_2 , the control variable u^* is taken as:

$$\begin{aligned} u^* = & u_{eq} - \hat{K}_{smc} \gamma \operatorname{sgn}(\sigma) \\ = & -(SB)^{-1} S \Lambda E - \hat{K}_{smc} \gamma \operatorname{sgn}(\sigma) \end{aligned} \quad (47)$$

where, $\hat{K}_{smc}$ is the estimated value of K_{smc}^* , and making the assumption that $\tilde{K}_{smc} = \hat{K}_{smc} - K_{smc}^*$, and also meeting the condition that $\tilde{K}_{smc} = \dot{\hat{K}}_{smc}$. Finally, the actual control variable u can be obtained from Eq. (23), as:

$$\begin{aligned} u = & (b_0 + \hat{b}_\Delta)^{-1} (k^T E + y_d^{(n)} - \hat{f}_0 - \hat{f}_\Delta \\ & + (SB)^{-1} S \Lambda E + \hat{K}_{smc} \gamma \operatorname{sgn}(\sigma)) \end{aligned} \quad (48)$$

The whole gain adaptive sliding mode controller (GASMC) based on an interval type-II fuzzy neural network (ITIIFNN) identification algorithm has been given in Fig. 2.

4.2 Stability Analysis

Theorem 1. Consider the error dynamic system Eq. (23),

if the control variable u is obtained by Eq. (48). Then, the adjustable parameters adaptive laws of ITIIFNN, and gain adaptive laws of sliding mode control, are chosen as:

$$\begin{aligned}\dot{\sigma}_{f\Delta} &= -\Gamma_{f\Delta} \sigma \frac{\partial \hat{f}_{\Delta}}{\partial \sigma_{f\Delta}} \\ \dot{\sigma}_{b\Delta} &= -\Gamma_{b\Delta} \sigma \frac{\partial \hat{b}_{\Delta}}{\partial \sigma_{b\Delta}} \\ \dot{\hat{K}}_{smc} &= \Gamma_{Ksmc} \gamma | \sigma | \end{aligned} \quad (49)$$

where, $\Gamma_{f\Delta} > 0, \Gamma_{b\Delta} > 0, \Gamma_{Ksmc} > 0$ denote the adaptive gain matrixes.

Proof. Define a Lyapunov function as:

$$\begin{aligned}V &= \frac{1}{2} \sigma^T (SB)^{-1} \sigma + \frac{1}{2} \Phi_{f\Delta}^T \Gamma_{f\Delta}^{-1} \Phi_{f\Delta} \\ &\quad + \frac{1}{2} \Phi_{b\Delta}^T \Gamma_{b\Delta}^{-1} \Phi_{b\Delta} + \frac{1}{2} \tilde{K}_{smc}^T \Gamma_{Ksmc}^{-1} \tilde{K}_{smc} \end{aligned} \quad (50)$$

Then, the time derivative of the Lyapunov function V becomes:

$$\begin{aligned}\dot{V} &= \sigma^T (SB)^{-1} \dot{\sigma} + \Phi_{f\Delta}^T \Gamma_{f\Delta}^{-1} \dot{\Phi}_{f\Delta} + \Phi_{b\Delta}^T \Gamma_{b\Delta}^{-1} \dot{\Phi}_{b\Delta} + \tilde{K}_{smc}^T \Gamma_{Ksmc}^{-1} \dot{\tilde{K}}_{smc} \\ &= \sigma^T (SB)^{-1} [S(AE + Bu^* + B\hat{h}_1 + B\hat{h}_2)] + \Phi_{f\Delta}^T \Gamma_{f\Delta}^{-1} \dot{\Phi}_{f\Delta} \\ &\quad + \Phi_{b\Delta}^T \Gamma_{b\Delta}^{-1} \dot{\Phi}_{b\Delta} + \tilde{K}_{smc}^T \Gamma_{Ksmc}^{-1} \dot{\tilde{K}}_{smc} \\ &= \sigma^T (SB)^{-1} S(AE + \sigma^T u^* + \sigma^T h_1 + \sigma^T h_2) + \Phi_{f\Delta}^T \Gamma_{f\Delta}^{-1} \dot{\Phi}_{f\Delta} \\ &\quad + \Phi_{b\Delta}^T \Gamma_{b\Delta}^{-1} \dot{\Phi}_{b\Delta} + \tilde{K}_{smc}^T \Gamma_{Ksmc}^{-1} \dot{\tilde{K}}_{smc} \end{aligned} \quad (51)$$

Using Eq. (44), Eq. (48) and Eq. (50), the time derivative of V can be derived as:

$$\dot{V} = -\sigma^T \hat{K}_{smc} \gamma \operatorname{sgn}(\sigma) + \sigma^T h_2 + \tilde{K}_{smc}^T \Gamma_{Ksmc}^{-1} \dot{\tilde{K}}_{smc} \quad (52)$$

And considering the inequality of Eq. (38), then the time derivative of V can be obtained as:

$$\begin{aligned}\dot{V} &\leq -\sigma^T \hat{K}_{smc} \gamma \operatorname{sgn}(\sigma) + \sigma^T K_{smc}^* + \tilde{K}_{smc}^T \Gamma_{Ksmc}^{-1} \dot{\tilde{K}}_{smc} \\ &\leq -\hat{K}_{smc} \gamma | \sigma | + K_{smc}^* \gamma | \sigma | + \tilde{K}_{smc}^T \Gamma_{Ksmc}^{-1} \dot{\tilde{K}}_{smc} \\ &= -(\hat{K}_{smc} - K_{smc}^*) \lambda | \sigma | + \tilde{K}_{smc}^T \Gamma_{Ksmc}^{-1} \dot{\tilde{K}}_{smc} \\ &= -\tilde{K}_{smc} (\gamma | \sigma | - \Gamma_{Ksmc}^{-1} \dot{\tilde{K}}_{smc}) \\ &\leq 0 \end{aligned} \quad (53)$$

This is to say that $\lim_{t \rightarrow \infty} \sigma = 0$, according to the Lyapunov stability theorem, because the switching surface is stable, then $\lim_{t \rightarrow \infty} E = 0$. In other words, the error dynamic system Eq. (23) is uniform asymptotic stable.

5. Experimental results

5.1 Experimental setup

A schematic view of the aerial control platform using TMS320F2812 is shown in Fig. 4. The Eight-Rotor MAV has

four blades, driven by eight BLDC motors, mounted at each end of the body frame. The Encoders were used for measuring the speed of each motor. The INS data are updated at 5 Hz, and the static pressure sensor measures are provided at a rate of 50 Hz. The low-cost IMU outputs raw data from 3 accelerometers, 3 gyro meters and 3 magnetometers to the flight control computer, which receives all these sensor data through an RS-232 serial port. The on-board flight control computer is TMS320F2812 (DSP), which runs at 29.4M Hz, with 512k flash memory, including eight serial ports, eight channels with programmable gains, 24-bit analog input, six programmable Pulse Width Modulation (PWM) outputs, and supports floating point calculations.

To avoid signal interference between sensor signals and the motors PWM, two independent power supplies are supplied. One battery is used to feed the eight electric motors, which are controlled using PWM, the other battery is used to feed the microcontroller and the sensors, and by adequate grounding, the interference is largely reduced.

5.2 Parameters setup

The Eight-Rotor Micro Aircraft Vehicle is characterized by a nominal main body inertia matrix :

$$J = \begin{bmatrix} 0.85 & 0 & 0 \\ 0 & 0.67 & 0 \\ 0 & 0 & 0.786 \end{bmatrix} \text{ kg} \cdot \text{m}^2$$

The fuzzy rules in the ITIIFNN can be generated automatically, by using the on-line adaptive laws to obtain suitable-structure neural networks, so the weighting factor is set to be zero $W_{f\Delta}^j = W_{g\Delta}^j = 0$ initially. The other parameters can be chosen as:

$$k_{\phi} = [150, 55, 12]^T; \quad k_{\theta} = [145, 65, 18]^T; \quad k_{\psi} = [160, 60, 22]^T;$$

$$Q_{\phi} = \operatorname{diag}(115, 115, 115); \quad Q_{\theta} = \operatorname{diag}(120, 120, 120);$$

$$Q_{\psi} = \operatorname{diag}(130, 130, 130).$$

The parameters of the sliding mode used here are chosen as:

$$K_{smc}(0) = [1.2 \times 10^5, 10^4]^T,$$

Fig. 4. Schematic view of aerial control platform using TMS320F2812

$$\Gamma_{smc} = \text{diag}(4.5 \times 10^4, 4.5 \times 10^4).$$

The initial attitude angle is set to be zero, $\theta_0 = 0, \phi_0 = 0, \psi_0 = 0$. The attitude perturbations are set to be a sine function, to reflect the changed attitude perturbations real-time, and

the perturbations are given as: $\tilde{\theta} = 0.3^\circ \sin \frac{\pi}{4} t$, $\tilde{\psi} = 0.5^\circ \sin \frac{\pi}{8} t$, $\tilde{\phi} = 0.2^\circ \sin \frac{\pi}{3} t$. Considering the torque perturbations caused

by the Micro Aircraft Vehicle body and Micro Aircraft Vehicle wing, the uncertainty functions are set to be $[0.2^\circ \cos t, 0.15^\circ \cos t, 0.1^\circ \cos t]^T$. The external flow has been taken into account, in the model used for simulation at $[0.3^\circ \sin t, 0.2^\circ \sin t, 0.1^\circ \sin t]^T$. The control objective is to control the attitude angle to track the reference trajectory, shown as:

$$\begin{cases} \psi = 25^\circ \\ \theta = 10^\circ \\ \phi = 5^\circ \end{cases} \quad 0 \leq t \leq 400 \text{ ms}$$

5.3. Experimental results

For the purpose of comparison, several different kinds of control scheme are conducted, to demonstrate the effectiveness of the proposed approach. We will apply the conventional adaptive sliding mode controller [21], a type-I fuzzy neural network based sliding mode controller [22-23] and an interval type-II fuzzy neural network identification based gain adaptive sliding mode controller, to let the Micro

Aircraft Vehicle system track the reference attitude trajectory.

The yaw Angle, pitch Angle and roll Angle, three attitude angles of trajectory tracking simulations, have been made as follows: Fig. 5 shows the trajectory tracking response curve of the three angles, under the circumstance without external disturbance and uncertainty. Fig. 6 shows the trajectory tracking response curve of the three angles, under the circumstance with external disturbance and uncertainty. Subscript Numbers under attitude Angles correspond to three kinds of controller: "1" is representative of the conventional adaptive sliding mode controller; "2" is representative of the type-I fuzzy neural network based sliding mode controller; and "3" is representative of the type-II fuzzy neural network identification based adaptive sliding mode controller.

The above two experimental results indicate that tracking performances can be guaranteed under the three different control schemes. The conventional adaptive sliding mode control scheme responds fast, but its overshoot is somewhat large; the Type-I fuzzy neural network based sliding mode control scheme has smaller steady-state error, but with longer regulation time; the Type-II fuzzy neural network identification based gain adaptive sliding mode control has better control accuracy, and smaller overshoot. The control accuracy decreases under uncertainty factors and external disturbances for all of the three control schemes, but could satisfy the performance standard of the control system; furthermore, the Type-II fuzzy neural network identification based gain adaptive sliding mode control scheme gives better performances, compared with the other ones.

(a) Response curves of pitch angle ψ

(b) Response curves of yaw angle lead-lag θ

(c) Response curves of roll angle ϕ

Fig. 5. Response curves of attitude angle

Arranging the above simulation results from Fig. 5 - Fig. 6, then the response data of the three attitude angles are listed in Table 1. From Fig. 5 - Fig. 6 and Table 1, we can see that not only from the nominal system, but also from the system with uncertainty and external disturbances in Fig. 6, it can be seen that the conventional adaptive sliding mode control scheme produces greater overshoot and steady-state error; the Type-I fuzzy neural network based sliding mode control scheme produces large overshoot and small steady-state error; and the Type-II fuzzy neural network identification based gain adaptive sliding mode control scheme produces smaller overshoot and small steady-state error.

6. Conclusions

In this paper, we have presented the dynamical modeling and intelligent control strategy of a MAV having eight rotors. One of the main characteristics of these configurations is the damage tolerance and increased stability in the wind. A novel adaptive sliding mode controller based on an interval type-II fuzzy neural network is developed, to handle uncertainties caused by both rule uncertainties and attitude angle perturbations, for an attitude angle control system involving external disturbances. The Lyapunov stability theorem has been used to test the asymptotic stability of the closed-loop system. Therefore, the parameters of the interval type-II fuzzy neural network and gain of the sliding mode control can be tuned on-line, by adaptive laws based on the Lyapunov

synthesis approach. From the experimental and comparison results, it is obvious that the tracking performance obtained from the proposed methodology is better than the type-I fuzzy neural network sliding mode controller and conventional adaptive sliding mode controller, not only in the nominal system, but also in the system with uncertainty factors and external disturbances. Thus, the experimental results have demonstrated the effectiveness of the proposed algorithm.

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(a) Response curves of pitch angle ψ

(b) Response curves of yaw angle lead-lag θ

(c) Response curves of roll angle ϕ

Fig. 6. Response curves of attitude angle

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